# ПАПIBIA UПIVERSITY <br> OF SCIEПCE AПD TECHחOLOGY <br> FACULTY OF HEALTH, APPLIED SCIENCES AND NATURAL RESOURCES <br> DEPARTMENT OF MATHEMATICS AND STATISTICS 

| QUALIFICATION: BACHELOR OF ECONOMICS |  |
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| QUALIFICATION CODE: 07BECO | LEVEL: 5 |
| COURSE CODE: MFE511S | COURSE NAME: MATHEMATICS FOR ECONOMISTS 1A |
| SESSION: JULY 2022 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS: 100 |


| SECOND OPPORTUNITY/SUPPLEMENTARY EXAMINATION QUESTION PAPER |  |
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| MODERATOR: | MR I.D.O NDADI |

## INSTRUCTIONS

1. Answer ALL the questions in the booklet provided.
2. Show clearly all the steps used in the calculations.
3. All written work must be done in blue or black ink and sketches must be done in pencil.
4. Decimal answers must be rounded to 4 decimals places

## PERMISSIBLE MATERIALS

1. Non-programmable calculator without a cover.

THIS QUESTION PAPER CONSISTS OF 4 PAGES (Including this front page)

## QUESTION 1 (25 marks)

1.1 For each of the following statements, indicate whether True (T) or False (F)
1.1.1 $\sqrt{\sqrt{(x-2)}}=|(x-2)|$
1.1.2 $\log _{b}\left(\frac{x}{b}\right)=\log _{b} x-1$
1.1.3 $\lim _{\delta \rightarrow 0} 5=5$
1.1.4 If $a^{2}+b^{2}=1$ and $x^{2}+y^{2}=2$, then $(a x+b y)^{2}+(a y-b x)^{2}=2$
1.1.5 $Q=0.001 K^{0.23} L^{0.76}$ is a strict Cobb-Douglas production function
1.2 Determine the degree of the polynomial.

$$
\begin{equation*}
\left(9 x^{2} y^{3} z\right)^{2}-\frac{6 x^{2} y}{\left(y^{-3} z^{-2}\right)^{3}}+11 x^{4} y z^{6}+\left(4 x y^{2} z\right)^{3} \tag{3}
\end{equation*}
$$

1.3 Simplify the expression $\frac{(a+b)^{2}-c^{2}}{a^{2}+a b+a c+b c} \times \frac{a^{2}+a b-a c-b c}{a+b+c} \div \frac{2 a^{2}-a c-c^{2}}{a^{2}-c^{2}}$
1.4 Solve the following indicial equation in $x:\left[\left(\frac{1}{20}\right)^{2+x} \times\left(\frac{1}{20}\right)^{8 . x}\right]^{2}=1$
1.5 Evaluate $\lim _{x \rightarrow 2} \frac{x^{2}-4}{x-2}$

1. 6 Use first principle of differentiation to evaluate $\frac{d y}{d x}$ if $y=x^{-1}$

## QUESTION 2 ( 30 marks)

2.1 Assume an income tax $\boldsymbol{T}$ with a proportional component $\boldsymbol{t}$ incorporated into an income determination model $Y=C+I$,

$$
C=C_{0}+b Y_{m}, T=T_{0}+t Y, Y_{m}=Y-T, I=I_{0}
$$

where $C_{0}=42, I_{0}=15, T_{0}=10, b=0.375$ and $t=0.2$
2.1.1 Determine the reduced form of this model
2.1.2 Determine the numerical value of $Y$
2.2 Given that $Q_{s}=-5+3 p$ and $Q_{d}=10-2 p$, determine the equilibrium price and quantity
2.3 The Investment-Savings (IS) and Liquidity Preference - Money Supply (LM) models of a certain 3-sector economy, $Y=C+I+G$, economy compose the following:
IS
$C=100+0.8 Y_{d} ; Y_{d}=Y-T$
$I=50-25 i$
$G=T=50$

$$
\begin{gathered}
L M \\
M^{d}=Y-25 i \ldots . . \text { demand } \\
\frac{M^{s}}{P}=200 \ldots \ldots . . . \text { supply }
\end{gathered}
$$

Derive the $I S$ and $L M$ equations and hence determine the equilibrium levels of income and rate of interest, where $P=2$.
2.4 A firm uses labour ( L ) and machines $(\mathrm{K})$ to manufacture their products. The cost of labour is $N \$ 40$ per unit and the cost of using a machine is $N \$ 10$.
2.4.1 Derive the budget line of the firm.
2.4.2 Sketch a budget line for this firm, showing the combinations of (L,K) with total cost of $N \$ 400$, label the budget line with $\left(C_{1}\right)$.
2.4.3 On the same graph, sketch another budget line with total cost of N\$200, label it with $\left(C_{2}\right)$
2.4.4 Discuss your observations between the two-budget lines.

## QUESTION 3 (25 marks)

3.1 A firm 's short-run production function is given by $Q=L e^{-0.02 L}$.
3.1.1 Find the marginal product of labour?
3.1.2 At $L=50$, determine whether the firm's maximes its production level?
3.1.3 What will be the production output at $L=50$ ?
3.2 Given the production

$$
Q=K^{2}+2 L^{2}
$$

3.2.1 Determine the marginal products of $\frac{\partial Q}{\partial K}$ and $\frac{\partial Q}{\partial L}$
3.2.2 Show that $M R T S=\frac{2 L}{K}$ and $K \frac{\partial Q}{\partial K}+L \frac{\partial Q}{\partial L}=2 Q$
3.3 Determine $\frac{d y}{d x}$, if $2 x^{3}-3 y^{2}+7 x y=0$

## QUESTION 4 (20 marks)

4.1 Determine the following integrals:

$$
\begin{array}{ll}
\text { 4.1.1 } & \int \sqrt{t} d t \\
\text { 4.1.2 } & \int_{0}^{5} e^{-2 x} d x
\end{array}
$$

4.2 Assume that the rate of an investment is given by the function $I(t)=6 \sqrt{t}$. Compute the total capital accumulation $(K)$ between the $1^{\text {st }}$ and $5^{\text {th }}$ years? [Hint: $\left.K=\int I(t) d t\right] \quad[6]$
4.3 The marginal revenue of a company is given $M R=100+20 x+3 x^{2}$, where $x$ is an amount of good in units sold for a period. Find the total revenue function at $(x=2)$ when total revenue is equal to 260 ?

